

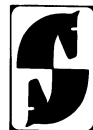
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Problems in Geometry

Translated by Silvio Levy

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