

31<sup>st</sup>  
EDITION

CRC  
**STANDARD** -  
**MATHEMATICAL**  
**TABLES AND**  
**FORMULAE**

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