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III.I.	Absolutely summing operators on the disc algebra Proper uniform algebras are uncomplemented, Bourgain's analytic projections onto $H_p(\Delta d\lambda)$, extrapolation inequalities between p -absolutely summing and q -integral norms for operators on A , A^* has cotype 2 and the Grothendieck theorem holds for A^* , extensions of finite rank operators on A , $A \widehat{\otimes} A$ is closed in $C(\mathbf{T}) \widehat{\otimes} C(\mathbf{T})$, reflexive subspaces of L_1/H_1 , extrapolation inequalities for the Riesz projection, extension of operators from reflexive subspaces of L_1/H_1 into H_∞ , interpolation for certain bi-analytic functions	291
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