

Martin A. Tanner

Tools for Statistical Inference

Methods for the Exploration of Posterior
Distributions and Likelihood Functions

Third Edition

With 47 Figures



Springer

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Mathematics Subject Classification: 62F15, 62Fxx, 62Jxx

Library of Congress Cataloging-in-Publication Data

Tanner, Martin Abba, 1957–

Tools for statistical inference: methods for the exploration of
posterior distributions and likelihood functions / Martin A. Tanner.
— 3rd ed.

p. cm. — (Springer series in statistics)

Includes bibliographical references and index.

ISBN-13: 978-1-4612-8471-0 e-ISBN-13: 978-1-4612-4024-2

DOI: 10.1007/978-1-4612-4024-2

1. Bayesian statistical decision theory. 2. Mathematical
statistics. I. Title. II. Series.

QA276.5.T36 1996

519.5'42—dc20

96-10784

Printed on acid-free paper.

© 1996 by Springer-Verlag New York, Inc.

Softcover reprint of the hardcover 3rd edition 1996

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Production managed by Hal Henglein, manufacturing coordinated by Jeffrey Taub.

Typeset by Bytheway Typesetting Services, Norwich, NY, using T_EX.

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