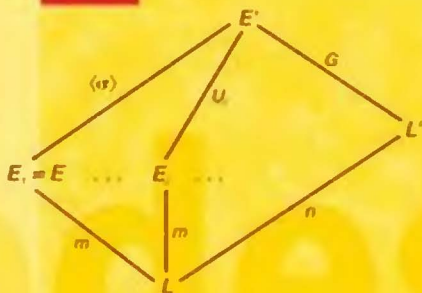


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# Algebraic Function Fields and Codes



Springer

University

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