

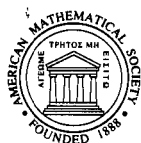
MATHEMATICAL Surveys and Monographs

Volume 41

Monotone Dynamical Systems

An Introduction to the Theory
of Competitive and Cooperative
Systems

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