

# Lecture Notes in Mathematics

A collection of informal reports and seminars

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Lectures  
on the Eilenberg-Moore  
Spectral Sequence

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