

# Lecture Notes in Mathematics

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# Asymptotic Behavior of Monodromy

Singularly Perturbed Differential Equations  
on a Riemann Surface

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## CONTENTS

<i>Introduction (I-XII)</i>	1
<b>1</b> <i>Ordinary differential equations on a Riemann surface</i>	12
<b>2</b> <i>Laplace transform, asymptotic expansions, and the method of stationary phase</i>	17
<b>3</b> <i>Construction of flows</i>	31
<b>4</b> <i>Moving relative homology chains</i>	41
<b>5</b> <i>The main lemma</i>	54
<b>6</b> <i>Finiteness lemmas</i>	60
<b>7</b> <i>Sizes of cells</i>	68
<b>8</b> <i>Moving the cycle of integration</i>	84
<b>9</b> <i>Bounds on multiplicities</i>	93
<b>10</b> <i>Regularity of individual terms</i>	101
<b>11</b> <i>Complements and examples</i>	111
<b>12</b> <i>The Sturm-Liouville problem</i>	127
<i>References</i>	135
<i>Index</i>	138