

Fibonacci's Liber Abaci

A Translation into Modern English of
Leonardo Pisano's Book of Calculation



Springer

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