

Joel L. Schiff

The Laplace Transform

Theory and Applications

With 68 Illustrations



Springer

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Mathematics Subject Classification (1991): 44A10

Library of Congress Cataloging-in-Publication Data

Schiff, Joel L.

The Laplace transform: theory and applications / Joel L. Schiff.

p. cm.—(Undergraduate texts in mathematics)

Includes bibliographical references and index.

ISBN 978-1-4757-7262-3 ISBN 978-0-387-22757-3 (eBook)

DOI 10.1007/978-0-387-22757-3

1. Laplace transformation. I. Title. II. Series.

QA432.S33 1999

515'.723—dc21

98-14037

Printed on acid-free paper.

© 1999 Springer Science+Business Media New York
Originally published by Springer-Verlag New York, Inc. in 1999
Softcover reprint of the hardcover 1st edition 1999

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Production managed by Robert Bruni; manufacturing supervised by Jeffrey Taub.
Typeset by The Bartlett Press, Inc., Marietta, GA.

9 8 7 6 5 4 3 2 1

ISBN 978-1-4757-7262-3

SPIN 10707361

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