

B.A. Rosenfeld

# A History of Non-Euclidean Geometry

Evolution of the Concept of  
a Geometric Space

Translated by Abe Shenitzer  
With the Editorial Assistance of Hardy Grant

With 114 Illustrations



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