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路易斯·步驰

有限群 **Blocks of**  
的块 **Finite Groups**

块的超聚焦 **The Hyperfocal Subalgebra**  
子代数 **of a Block**



Springer

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