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**MATHEMATICAL &  
COMPUTATIONAL TOOLS IN  
METROLOGY & TESTING VIII**

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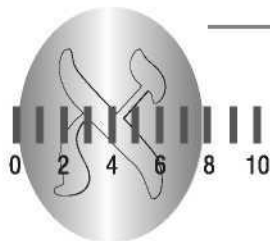
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*Published by*

World Scientific Publishing Co. Pte. Ltd.

5 Toh Tuck Link, Singapore 596224

USA office: 27 Warren Street, Suite 401-402, Hackensack, NJ 07601

UK office: 57 Shelton Street, Covent Garden, London WC2H 9HE

**Library of Congress Cataloging-in-Publication Data**

AMCTM VIII (2008 : Paris, France)

Advanced mathematical and computational tools in metrology and testing : AMCTM VIII /  
edited by Franco Pavese ... [et al.].

p. cm. -- (Series on advances in mathematics for applied sciences ; v. 78)

Includes index.

ISBN-13: 978-981-283-951-0 (hardcover : alk. paper)

ISBN-10: 981-283-951-8 (hardcover : alk. paper)

1. Measurement--Congresses. 2. Physical measurements--Congresses. 3. Metrology--Congresses.  
I. Pavese, Franco. II. Title. III. Title: AMCTM 8.

QA465.A58 2008

530.8--dc22

2009001775

**British Library Cataloguing-in-Publication Data**

A catalogue record for this book is available from the British Library.

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Printed in Singapore.

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