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Editors

Recent Developments in Domain Decomposition Methods

With 69 Figures, 13 in Color, and 54 Tables



Springer

Editors

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