A.N. Parshin I. R. Shafarevich (Eds.)

# Algebraic Geometry V

Fano Varieties



Springer

## **Fano Varieties**

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#### Contents

Intro	duction	4
Chap	ter 1. Preliminaries	7
§1.1.	Singularities	7
-	On Numerical Geometry of Cycles	
-	On the Mori Minimal Model Program	
§1.4.	Results on Minimal Models in Dimension Three	17
Chap	ter 2. Basic Properties of Fano Varieties	23
§2.1.	Definitions, Examples and the Simplest Properties	23
	Some General Results	34
	Existence of Good Divisors in the Fundamental Linear System	39
	Base Points in the Fundamental Linear System	47
Chap	ter 3. Del Pezzo Varieties and Fano Varieties of Large Index	50
§3.1.	On Some Preliminary Results of Fujita	50
-	Del Pezzo Varieties. Definition and Preliminary Results	53
§3.3.	Nonsingular del Pezzo Varieties. Statement of the Main Theorem	
-	and Beginning of the Proof	54
§3.4.	Del Pezzo Varieties with Picard Number $\rho = 1$ .	
0	Continuation of the Proof of the Main Theorem	57
§3.5.	Del Pezzo Varieties with Picard Number $\rho \geq 2$ .	
	Conclusion of the Proof of the Main Theorem	62

Chapter 4. Fano Threefolds with $\rho = 1$			
<ul> <li>§4.1. Elementary Rational Maps: Preliminary Results</li></ul>			
Chapter 5. Fano Varieties of Coindex 3 with $\rho = 1$ : The Vector Bundle Method			
<ul> <li>§5.1. Fano Threefolds of Genus 6 and 8: Gushel's Approach</li></ul>			
Chapter 6. Boundedness and Rational Connectedness of Fano Varieties			
<ul><li>§6.1. Uniruledness</li></ul>			
Chapter 7. Fano Varieties with $\rho \geq 2$			
<ul> <li>§7.1. Fano Threefolds with Picard Number ρ ≥ 2 (Survey of Results of Mori and Mukai</li></ul>			
Chapter 8. Rationality Questions for Fano Varieties I			
<ul> <li>§8.1. Intermediate Jacobian and Prym Varieties</li></ul>			
Chapter 9. Rationality Questions for Fano Varieties II			
<ul> <li>§9.1. Birational Automorphisms of Fano Varieties</li></ul>			
Chapter 10. Some General Constructions of Rationality and Unirationality			
<ul> <li>§10.1. Some Constructions of Unirationality</li></ul>			

#### Contents

Chapter 11. Some Particular Results and Open Problems			
<ul> <li>§11.1. On the Classification of Three-dimensional Q-Fano Varieties 196</li> <li>§11.2. Generalizations</li></ul>			
Chapter 12. Appendix: Tables			
References			
Index			

.

.1