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A. N. Parshin I. R. Shafarevich (Eds.)

# Algebra VII

Combinatorial Group Theory  
Applications to Geometry

With 39 Figures



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