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Analytic Number Theory and Diophantine Problems

Proceedings of a Conference at Oklahoma State University, 1984

Edited by
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PREFACE

A conference on Analytic Number Theory and Diophantine Problems was held from June 24 to July 3, 1984 at the Oklahoma State University in Stillwater. The conference was funded by the National Science Foundation, the College of Arts and Sciences and the Department of Mathematics at Oklahoma State University.

The papers in this volume represent only a portion of the many talks given at the conference. The principal speakers were Professors E. Bombieri, P. X. Gallagher, D. Goldfeld, S. Graham, R. Greenberg, H. Halberstam, C. Hooley, H. Iwaniec, D. J. Lewis, D. W. Masser, H. L. Montgomery, A. Selberg, and R. C. Vaughan. Of these, Professors Bombieri, Goldfeld, Masser, and Vaughan gave three lectures each, while Professor Hooley gave two. Special sessions were also held and most participants gave talks of at least twenty minutes each. Prof. P. Sarnak was unable to attend but a paper based on his intended talk is included in this volume.

We take this opportunity to thank all participants for their (enthusiastic) support for the conference. Judging from the response, it was deemed a success.

As for this volume, I take responsibility for any typographical errors that may occur in the final print. I also apologize for the delay (which was due to the many problems incurred while retyping all the papers).

A special thanks to Dollee Walker for retyping the papers and to Prof. W. H. Jaco for his support, encouragement and hard work in bringing the idea of the conference to fruition.

A. Ghosh

(on behalf of the Editors).

TABLE OF CONTENTS

K. ALLADI, P. ERDÖS and J. D. VAALER :.....1
Multiplicative functions and small divisors.

E. BOMBIERI :.....15
Lectures on the Thue Principle.

E. BOMBIERI and J. D. VAALER :.....53
Polynomials with low height and prescribed vanishing.

W. W. L. CHEN :.....75
On the irregularities of distribution and
approximate evaluation of certain functions II.

J. B. CONREY, A. GHOSH and S. M. GONEK :.....87
Simple zeros of the zeta-function of a quadratic
number field II.

H. DIAMOND, H. HALBERSTAM and H.-E. RICHERT :.....115
Differential difference equations associated with
sieves.

J. FRIEDLANDER :.....125
Primes in arithmetic progressions and related
topics.

P. X. GALLAGHER :.....135
Applications of Guinand´s formula

D. GOLDFELD (appendix by S. FRIEDBERG) :.....159
Analytic number theory on GL(r,**R**).

D. A. GOLDSTON and H. L. MONTGOMERY :.....183
Pair correlation and primes in short intervals.

S. W. GRAHAM and G. KOLESNIK :.....205
One and two dimensional exponential sums.

R. GREENBERG :.....223
Non-vanishing of certain values of L-functions.

G. HARMAN :.....237
On averages of exponential sums over primes.

D. HENSLEY :.....247
The distribution of $\Omega(n)$ among numbers with no large prime factors.

T. KANO :.....283
On the size of $\sum_{n\leq x} d(n)e(nx)$

D. W. MASSER and G. WUSTHOLZ :.....291
Another note on Baker's Theorem.

M. B. NATHANSON :.....305
Sums of polygonal numbers.

A. D. POLLINGTON :.....317
On the density of B_2-bases.

P. SARNAK :.....321
Statistical properties of eigenvalues of the Hecke operators.

H.-B. SIEBURG :.....333
Transcendence theory over non-local fields.

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Alladi, K.
Bateman, P.
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Cooper, C.
Diamond, H. G.
Friedlander, J.
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Greenberg, R.
Gupta, R.
Halberstam, H.
Harman, G.
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Hildebrand, A.
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Iwaniec, H.
Jaco, W.
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Ng, E.
Pollington, A.
Schumer, P.
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