

METHODS BASED ON THE  
WIENER-HOPF TECHNIQUE

*for the solution of partial  
differential equations*

by

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