

John Lawrence Nazareth

An Optimization Primer

On Models, Algorithms, and Duality

With 28 Illustrations

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Springer

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