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COLLECTED PAPERS OF  
**JOHN  
MILNOR**

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II

**The Fundamental Group**



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American Mathematical Society

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2000 *Mathematics Subject Classification.* Primary 01A75;  
Secondary 53–03, 55–03, 57–03.

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### Library of Congress Cataloging-in-Publication Data

Milnor, John Willard, 1931–

The fundamental group.

p. cm. — (Collected papers of John Milnor : 2)

Originally published: Houston, Tex. : Publish or Perish, 1995.

ISBN 978-0-8218-4875-3 (alk. paper)

1. Knot theory. 2. Torsion. 3. Three-manifolds (Topology) I. Title.

QA612.2.M556 2009

514'.2242—dc22

2009019321

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Printed in the United States of America.

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10 9 8 7 6 5 4 3 2 1      14 13 12 11 10 09

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