

# Lecture Notes in Mathematics

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Robert A. McCoy  
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Topological Properties  
of Spaces of  
Continuous Functions

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## TABLE OF CONTENTS

	Page
<b>INTRODUCTION.....</b>	<b>1</b>
<b>I. FUNCTION SPACE TOPOLOGIES.....</b>	<b>3</b>
1. Set-open Topologies.....	3
2. Uniform Topologies.....	7
3. Exercises and Problems.....	13
<b>II. NATURAL FUNCTIONS.....</b>	<b>15</b>
1. Injections and Diagonal Functions.....	15
2. Composition Functions and Induced Functions.....	16
3. Evaluation Functions.....	23
4. Product Functions and Sum Functions.....	26
5. Exponential Functions.....	30
6. Exercises and Problems.....	35
<b>III. CONVERGENCE AND COMPACT SUBSETS.....</b>	<b>39</b>
1. Convergence.....	39
2. Compact Subsets.....	43
3. Exercises and Problems.....	47
<b>IV. CARDINAL FUNCTIONS.....</b>	<b>51</b>
1. Netweight.....	51
2. Density and Cellularity.....	53
3. Pseudocharacter.....	56
4. Character.....	57
5. Weight.....	60
6. Weak Weight.....	61
7. Tightness and the Frechet Property.....	62

8. Hereditary Density and Hereditary Lindelof Degree.....	65
9. Exercises and Problems.....	68
V. COMPLETENESS AND OTHER PROPERTIES.....	74
1. Uniform Completeness.....	74
2. $\check{\text{C}}$ ech-completeness and Complete Metrizability.....	75
3. Baire Spaces.....	77
4. An Application of Completeness.....	84
5. Countably Compact Subsets.....	88
6. Dense Subsets.....	91
7. Analytic Spaces.....	95
8. Exercises and Problems.....	100
HISTORICAL NOTES.....	106
BIBLIOGRAPHY.....	109
LIST OF SYMBOLS.....	120
SUBJECT INDEX.....	121