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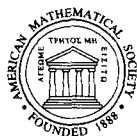
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Volume 12

**Symmetric Functions  
and Orthogonal Polynomials**

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