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The Hybrid Multiscale Simulation Technology

An Introduction
with Application to Astrophysical
and Laboratory Plasmas

With 124 Figures



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