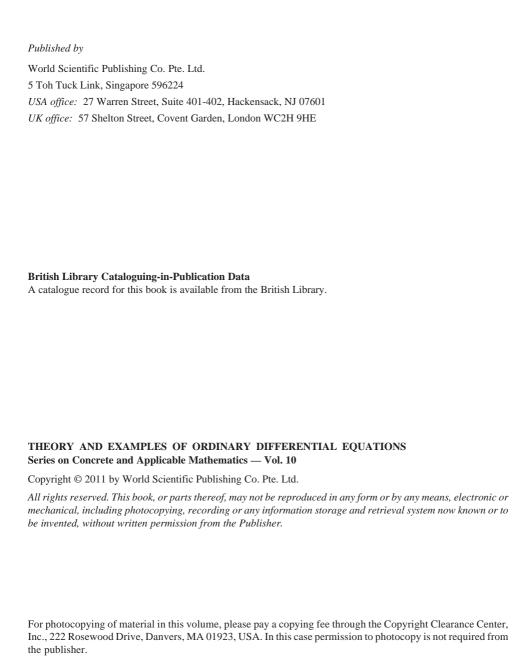
THEORY AND EXAMPLES OF ORDINARY DIFFERENTIAL EQUATIONS

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