

FOUNDATIONS OF ANALYSIS

THE ARITHMETIC OF
WHOLE, RATIONAL, IRRATIONAL
AND COMPLEX NUMBERS

*A Supplement to Text-Books on the
Differential and Integral Calculus...*

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