

57910

..
...
...

DIFFERENTIAL AND INTEGRAL CALCULUS

BY

EDMUND LANDAU

PROFESSOR OF MATHEMATICS

GOTTINGEN UNIVERSITY

TRANSLATED FROM THE GERMAN BY

MELVIN HAUSNER

AND

MARTIN DAVIS

AMS CHELSEA PUBLISHING

American Mathematical Society • Providence, Rhode Island

TABLE OF CONTENTS

Preface	1
Introduction	7
§ 1. Residue Classes	13
§ 2. The Decimal System	15
§ 3. Finite and Infinite Sets of Numbers.....	18

PART ONE

DIFFERENTIAL CALCULUS

CHAPTER 1	
Limits as $n = \infty$	23
CHAPTER 2	
Logarithms, Powers, and Roots.....	39
CHAPTER 3	
Functions and Continuity.....	49
CHAPTER 4	
Limits as $x = \xi$	61
CHAPTER 5	
Definition of the Derivative.....	69
CHAPTER 6	
General Theorems on the Formation of the Derivative.....	79
CHAPTER 7	
Increase, Decrease, Maximum, Minimum.....	87
CHAPTER 8	
General Properties of Continuous Functions on Closed Intervals.....	92
CHAPTER 9	
Rolle's Theorem and the Theorem of the Mean.....	108

	CHAPTER 10	
Derivatives of Higher Order; Taylor's Theorem.....		115
	CHAPTER 11	
"0/0" and Similar Matters.....		128
	CHAPTER 12	
Infinite Series.....		146
	CHAPTER 13	
Uniform Convergence.....		168
	CHAPTER 14	
Power Series.....		179
	CHAPTER 15	
Exponential Series and Binomial Series.....		189
	CHAPTER 16	
The Trigonometric Functions.....		191
	CHAPTER 17	
Functions of Two Variables and Partial Derivatives.....		208
	CHAPTER 18	
Inverse Functions and Implicit Functions.....		223
	CHAPTER 19	
The Inverse Trigonometric Functions.....		229
	CHAPTER 20	
Some Necessary Algebraic Theorems.....		233
§ 1. The Fundamental Theorem of Algebra.....		233
§ 2. Decomposition of Rational Functions into Partial Fractions.....		243

PART TWO

INTEGRAL CALCULUS

	CHAPTER 21	
Definition of the Integral.....		253
	CHAPTER 22	
Basic Formulas of the Integral Calculus.....		259
	CHAPTER 23	
The Integration of Rational Functions.....		264

	CHAPTER 24	
The Integration of Certain Non-rational Functions.....		270
	CHAPTER 25	
Concept of the Definite Integral.....		280
	CHAPTER 26	
Theorems on the Definite Integral.....		289
	CHAPTER 27	
The Integration of Infinite Series.....		314
	CHAPTER 28	
The Improper Integral		319
	CHAPTER 29	
The Integral with Infinite Limits		334
	CHAPTER 30	
The Gamma Function		348
	CHAPTER 31	
Fourier Series		357
INDEX OF DEFINITIONS		367
SUBJECT INDEX		369