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> Linear and Quasi-linear Equations of Parabolic Type



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ЛИНЕЙНЫЕ И КВАЗИЛИНЕЙНЫЕ УРАВНЕНИЯ ПАРАБОЛИЧЕСКОГО ТИПА

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