

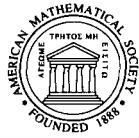
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Lebesgue Theory in the Bidual of $C(X)$

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