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Complex Systems: Chaos and Beyond

A Constructive Approach
with Applications in Life Sciences

With 111 Figures



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