

# Finite Fields and Applications



Dieter Jungnickel  
Harald Niederreiter  
*Editors*

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Proceedings of The Fifth International Conference  
on Finite Fields and Applications  $F_q5$ ,  
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# Preface

This volume represents the refereed proceedings of the Fifth International Conference on Finite Fields and Applications ( $\mathbf{F}_q5$ ) held at the University of Augsburg (Germany) from August 2–6, 1999, and hosted by the Department of Mathematics. The conference continued a series of biennial international conferences on finite fields, following earlier conferences at the University of Nevada at Las Vegas (USA) in August 1991 and August 1993, the University of Glasgow (Scotland) in July 1995, and the University of Waterloo (Canada) in August 1997. The Organizing Committee of  $\mathbf{F}_q5$  comprised Thomas Beth (University of Karlsruhe), Stephen D. Cohen (University of Glasgow), Dieter Jungnickel (University of Augsburg, Chairman), Alfred Menezes (University of Waterloo), Gary L. Mullen (Pennsylvania State University), Ronald C. Mullin (University of Waterloo), Harald Niederreiter (Austrian Academy of Sciences), and Alexander Pott (University of Magdeburg).

The program of the conference consisted of four full days and one half day of sessions, with 11 invited plenary talks and over 80 contributed talks that required three parallel sessions. This documents the steadily increasing interest in finite fields and their applications. Finite fields have an inherently fascinating structure and they are important tools in discrete mathematics. Their applications range from combinatorial design theory, finite geometries, and algebraic geometry to coding theory, cryptology, and scientific computing. A particularly fruitful aspect is the interplay between theory and applications which has led to many new perspectives in research on finite fields. This interplay has always been a dominant theme in  $\mathbf{F}_q$  conferences and was very much in evidence at  $\mathbf{F}_q5$ . Applied or applications-oriented topics accounted for well over half of the program.

These proceedings reflect the wide variety of topics represented at the conference. Most invited talks and a good proportion of the contributed talks are on permanent record here. All contributed talks were screened before the conference and all full papers were carefully refereed. We take this opportunity to thank the members of the Organizing Committee and all referees who helped in these tasks. These colleagues contributed enormously to the quality of the conference presentations and to guaranteeing high standards for these proceedings.

We greatly appreciate the generous financial support received for the conference. A major portion of the funds came from a grant by the German Research Council (DFG). Further sponsors were Andersen Consulting, Certicom Corp., Dresdner Bank AG, Gesellschaft der Freunde der Universität Augsburg, Hewlett Packard Laboratories, and Siemens AG. We are grateful to the University of Augsburg for providing excellent facilities for the conference and to the various officials of the City of Augsburg who helped with

organizational questions. Thanks are also due to the Mayor of Augsburg who gave a reception for the participants in the splendid setting of the Great Golden Chamber of the city's renaissance town hall. Last but not least, the highly efficient and friendly manner in which the conference took place would not have been possible without the enthusiasm and hard work by the assistants, secretaries and students who saw to the many details involved in such a major event; we are grateful to all of them.

Regarding the present proceedings, we thank Dr. Martin Peters of Springer Verlag who gave us the opportunity to place this volume with a top publisher and in a form which we find both attractive and practical (no rapidly deteriorating soft covers for once!). The cooperation with him and all the staff at Springer Verlag was always a pleasure.

Finally, we are pleased to confirm that the series of  $\mathbf{F}_q$  conferences will continue with  $\mathbf{F}_q6$  in Mexico in May 2001. We expect another lively and stimulating conference there, which should, like the previous conferences, serve as an important marketplace of ideas for the finite fields community.

October 2000

Dieter Jungnickel  
Harald Niederreiter

# Contents

Projective Generalized Reed-Muller Codes over $p$ -adic Numbers and Finite Rings . . . . .	1
<i>Kanat Abdukhalikov</i>	
Towards a Basis for the Space of Regular Functions in a Tower of Function Fields Meeting the Drinfeld-Vladut Bound . . . . .	14
<i>Iliia Aleshnikov, Vinay Deolalikar, P. Vijay Kumar, Henning Stichtenoth</i>	
Self-Dual Normal Bases and Related Topics . . . . .	25
<i>Eva Bayer-Fluckiger*</i>	
Permutations amongst the Dembowski-Ostrom Polynomials . . . . .	37
<i>Aart Blokhuis, Robert S. Coulter, Marie Henderson, Christine M. O’Keefe</i>	
Associative Rational Functions in Two Variables . . . . .	43
<i>Joel V. Brawley, Shuhong Gao* and Donald Mills</i>	
A Note on the Minimal Polynomial of the Product of Linear Recurring Sequences . . . . .	57
<i>Emrah Çakçak</i>	
Gelfond-Gramain’s Theorem for Function Fields . . . . .	70
<i>Mireille Car</i>	
On Generalized Bent and $q$ -ary Perfect Nonlinear Functions . . . . .	81
<i>Claude Carlet, Sylvie Dubuc</i>	
Divisible Designs Admitting, as an Automorphism Group, an Orthogonal Group or a Unitary Group . . . . .	95
<i>Cinzia Cerroni, Ralph-Hardo Schulz</i>	
A Permutation of a Small Infinite Field . . . . .	109
<i>Stephen D. Cohen</i>	
Almost Perfect Nonlinear Power Functions on $\text{GF}(2^n)$ : A New Case for $n$ Divisible by 5 . . . . .	113
<i>Hans Dobbertin</i>	
On Non-Abelian Semi-Regular Relative Difference Sets . . . . .	122
<i>Dominic Elvira, Yutaka Hiramine</i>	

Applications of Arithmetical Geometry to Cryptographic Constructions 128 <i>Gerhard Frey*</i>	
Gauß Periods in Finite Fields . . . . . 162 <i>Joachim von zur Gathen*, Igor Shparlinski</i>	
Constructions of Orthomorphisms of $\mathbb{Z}_2^n$ . . . . . 178 <i>Solomon W. Golomb, Guang Gong, Lothrop Mittenthal</i>	
Period Polynomials for $F_{p^2}$ of Fixed Small Degree . . . . . 196 <i>Stanley Gurak</i>	
Universal Generators for Primary Closures of Galois Fields . . . . . 208 <i>Dirk Hachenberger*</i>	
Irreducible Polynomials Generated by Decimations . . . . . 224 <i>Fritz von Haeseler and Wibke Jürgensen</i>	
Decoding Reed-Muller Codes beyond Half the Minimum Distance . . . . . 232 <i>Agnes E. Heydtmann, Thomas Jakobsen</i>	
On Binary Cyclic Codes With Few Weights . . . . . 251 <i>Henk D. L. Hollmann, Qing Xiang*</i>	
MacWilliams Identities for Linear Codes over Finite Frobenius Rings . . 276 <i>Thomas Honold, Ivan Landjev</i>	
Cyclotomic Function Fields with Many Rational Places . . . . . 293 <i>Alice Keller</i>	
On the Siamese Twin Designs . . . . . 303 <i>H. Kharaghani</i>	
On the Brauer Monoid for Finite Fields . . . . . 313 <i>Vladimir V. Kirichenko, Boris V. Novikov</i>	
Algorithms for Factoring Polynomials over Finite Fields . . . . . 319 <i>Tanja Lange, Arne Winterhof</i>	
Gauss Sums over Quasi-Frobenius Rings . . . . . 329 <i>Philippe Langevin, Patrick Solé</i>	
On the Early History of Galois Fields . . . . . 341 <i>Heinz Lüneburg*</i>	
Linear Blocking Sets: a Survey . . . . . 356 <i>Guglielmo Lunardon, Olga Polverino</i>	



Comparison of Techniques on Divisibility Properties of Exponential Sums and Applications .....	363
<i>Oscar Moreno*, Francis N. Castro</i>	
On the Rank of Appearance and the Number of Zeros of the Lucas Sequences over $\mathbb{F}_q$ .....	390
<i>Siguna Müller</i>	
A Permutation Problem for Finite Fields .....	409
<i>Alan R. Prince</i>	
The $L$ -Function of Gold Exponential Sum .....	418
<i>Kenneth Shum, P. Vijay Kumar, Tor Helleseth</i>	
On Permutation Polynomials and Derivable Translation Planes .....	428
<i>Rita Vincenti</i>	
Pure $L$ -Functions from Algebraic Geometry over Finite Fields .....	437
<i>Daqing Wan*</i>	
Incomplete Additive Character Sums and Applications .....	462
<i>Arne Winterhof</i>	
Applications of Algebraic Curves to Constructions of Codes and Almost Perfect Sequences .....	475
<i>Chaoping Xing*, Harald Niederreiter</i>	
<b>Author Index</b> .....	490

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\* invited speaker