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Mathematical Modeling in Biomedical Imaging I

Electrical and Ultrasound Tomographies,
Anomaly Detection, and Brain Imaging

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