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Quantum Independent Increment Processes II

Structure of Quantum Lévy Processes,
Classical Probability, and Physics

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Random Walks on Finite Quantum Groups

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