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The Analysis of Linear Partial Differential Operators II

Differential Operators
with Constant Coefficients



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