

# LEONHARDI EULERI OPERA OMNIA

SUB AUSPICIIS SOCIETATIS SCIENTIARUM NATURALIUM HELVETICAE

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SERIES PRIMA · OPERA MATHEMATICA · VOLUMEN QUARTUM

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## LEONHARDI EULERI COMMENTATIONES ARITHMETICAE

VOLUMEN TERTIUM

EDIDIT

RUDOLF FUETER

AUCTORITATE ET IMPENSIS  
SOCIETATIS SCIENTIARUM NATURALIUM HELVETICAE

GENEVAE MCMXLI

VENDITIONI EXPONUNT  
ORELL FÜSSLER TURICI ET LIPSIAE  
B. G. TEUBNER LIPSIAE ET BEROLINI

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