

ON THE
SENSATIONS OF TONE

AS A PHYSIOLOGICAL BASIS FOR THE
THEORY OF MUSIC

HERMANN L. F. HELMHOLTZ

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with numerous additional Notes and a New additional Appendix
bringing down information to 1885, and especially
adapted to the use of Music Students by
ALEXANDER J. ELLIS*

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