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Monographs and Surveys in  
Pure and Applied Mathematics

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**VARIATIONAL AND**

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**POTENTIAL METHODS**

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**IN THE THEORY OF**

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**BENDING OF PLATES WITH**

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**TRANSVERSE SHEAR**

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**DEFORMATION**

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CHRISTIAN CONSTANDA

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