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115

VARIATIONAL AND
POTENTIAL METHODS
IN THE THEORY OF
BENDING OF PLATES WITH
TRANSVERSE SHEAR
DEFORMATION

IGOR CHUDINOVICH
CHRISTIAN CONSTANDA

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