

# Harmonic Analysis and Partial Differential Equations

*Essays in Honor of Alberto P. Calderón*

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