## CONTEMPORARY MATHEMATICS

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## Computability Theory and Its Applications

Current Trends and Open Problems

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