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The Red Book of Varieties and Schemes

Second, Expanded Edition

Includes the Michigan Lectures (1974)
on Curves and their Jacobians



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Table of Contents

Preface to the Second Edition	V
Preface to the First Edition	VII
Table of Contents	IX
I. Varieties	1
§1. Some algebra	1
§2. Irreducible algebraic sets	5
§3. Definition of a morphism	11
§4. Sheaves and affine varieties	16
§5. Definition of prevarieties and morphisms	25
§6. Products and the Hausdorff Axiom	33
§7. Dimension	40
§8. The fibres of a morphism	48
§9. Complete varieties	54
§10. Complex varieties	57
II. Preschemes	65
§1. $\text{Spec } (R)$	66
§2. The category of preschemes	77
§3. Varieties and preschemes	86
§4. Fields of definition	94
§5. Closed subpreschemes	103
§6. The functor of points of a prescheme	112
§7. Proper morphisms and finite morphisms	121
§8. Specialization	127
III. Local Properties of Schemes	137
§1. Quasi-coherent modules	138
§2. Coherent modules	146
§3. Tangent cones	153
§4. Non-singularity and differentials	164
§5. Étale morphisms	174
§6. Uniformizing parameters	183

§7. Non-singularity and the UFD property	187
§8. Normal varieties and normalization	196
§9. Zariski's Main Theorem	207
§10. Flat and smooth morphisms	214
Appendix: Curves and Their Jacobians	225
Lecture I: What is a Curve and How Explicitly Can We Describe Them?	229
Lecture II: The Moduli Space of Curves: Definition, Coordinatization, and Some Properties	243
Lecture III: How Jacobians and Theta Functions Arise	257
Lecture IV: The Torelli Theorem and the Schottky Problem	271
Survey of Work on the Schottky Problem up to 1996 by Enrico Arbarello	287
References: The Red Book of Varieties and Schemes	293
Guide to the Literature and References:	
Curves and Their Jacobians	294
Supplementary Bibliography on the Schottky Problem	
by Enrico Arbarello	301