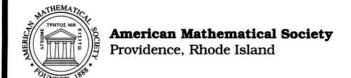
Translations of MATHEMATICAL MONOGRAPHS

Volume 160

Linear and Nonlinear Perturbations of the Operator div

V. G. Osmolovskiĭ



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