

AN ATLAS OF GRAPHS

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Italic entries refer to the pictures of graphs

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Index of abbreviations

We list here the abbreviations for the various types of graphs depicted in this *Atlas*.

A	acyclic digraphs	298
B	connected bipartite graphs	191
Bc	connected bicubic graphs	157
Bn	binary trees	101
C	connected cubic graphs	127
Cp	convex cubic polyhedral graphs	159
Ct	connected cubic transitive graphs	161
D	digraphs	292
E	Eulerian graphs	197
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F	connected quintic graphs	154
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H	homeomorphically irreducible trees	84
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