

**PROBLEM BOOK**

**IN THE  
THEORY OF FUNCTIONS**

**Volume I**  
*Problems in the Elementary Theory of Functions*

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