

2
2.7
2.71
2.718
2.7182
2.71828
2.718281
2.7182818
2.71828182
2.718281828
2.7182818284

e

*The Story
of a Number*

ELI MAOR

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