

D. V. Anosov (Ed.)

Dynamical Systems IX

Dynamical Systems
with Hyperbolic Behaviour

With 39 Figures



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Dynamical Systems with Hyperbolic Behaviour

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Contents

Preface (<i>D.V. Anosov</i>)	4
References	9
Chapter 1. Hyperbolic Sets (<i>D.V. Anosov, V.V. Solodov</i>)	10
§1. Preliminary Notions	10
1.1. Definition of a Hyperbolic Set	10
1.2. Comments	16
1.3. Stable and Unstable Manifolds	21
1.4. Stable and Unstable Manifolds in Certain Special Cases	27
§2. Some Examples	31
2.1. Heteroclinic and Homoclinic Points	31
2.2. The Smale Horseshoe	34
2.3. Motions in a Neighbourhood of a Homoclinic Trajectory. ϵ -Trajectories	46
2.4. Markov Partitioning for a Hyperbolic Automorphism of a Two-Dimensional Torus	51

2.2. Topological Classification of A -diffeomorphisms with Non-trivial Basic Sets and Homeomorphisms with Two Invariant Transversal Foliations	149
§3. Various Approaches to the Problem of the Realization of Homotopy Classes of Homeomorphisms with Given Topological Properties	157
3.1. Geodesic Laminations and Their Role in the Construction of Representatives of Homotopy Classes of Homeomorphisms ..	157
3.2. The Nielsen-Thurston Theory on the Homotopy Classification of Homeomorphisms of Surfaces	164
References	171
Chapter 4. Dynamical Systems with Transitive Symmetry Group. Geometric and Statistical Properties (<i>A.V. Safonov, A.N. Starkov, A.M. Stepin</i>)	
Introduction	177
§1. Basic Concepts and Constructions. Examples	179
§2. A Criterion for Ergodicity and the Ergodic Decomposition	185
§3. Spectrum of Ergodic Flows on Homogeneous Spaces	192
§4. Orbits of Homogeneous Flows	199
§5. Statistical Properties of G -Induced Flows (and Actions)	207
§6. Rigidity of Homogeneous Flows	213
Appendix A. Structure of Spaces of Finite Volume	217
Appendix B. Construction of Semisimple Splitting of Simply Connected Lie Groups	222
Added to the English Translation	224
References	225
Author Index	231
Subject Index	233