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Local Methods in Nonlinear Differential Equations

Part I

The Local Method of Nonlinear Analysis
of Differential Equations

Part II

The Sets of Analyticity of a
Normalizing Transformation

Translated from the Russian
by William Hovsing and Courtney S. Coleman

With 94 Figures



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Introduction to the English Edition by Dr. Steven Wiggins	V
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