

Local representation theory

*Modular representations as an
introduction to the local representation
theory of finite groups*

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Contents

| | | |
|----------------------------------|-------------|-----|
| Preface | <i>page</i> | ix |
| I Semisimple modules | | |
| 1 Simple modules | | 1 |
| 2 Simple algebras | | 7 |
| 3 Group algebras | | 12 |
| | | |
| II Projective modules | | |
| 4 Indecomposable modules | | 21 |
| 5 Free modules | | 28 |
| 6 Duality | | 38 |
| 7 Tensor products | | 45 |
| | | |
| III Modules and subgroups | | |
| 8 Induced modules | | 54 |
| 9 Vertices and sources | | 65 |
| 10 Trivial intersections | | 70 |
| 11 Green correspondence | | 79 |
| 12 Maps | | 84 |
| | | |
| IV Blocks | | |
| 13 Defect groups | | 92 |
| 14 Brauer correspondence | | 101 |
| 15 Canonical module | | 105 |
| 16 Subpairs | | 112 |

| | |
|--------------------------------|-----|
| V Cyclic blocks | |
| 17 Brauer trees | 118 |
| 18 Nilpotent blocks | 128 |
| 19 Local case | 134 |
| 20 Projective covers | 143 |
| 21 Simple modules | 150 |
| 22 Brauer graph | 159 |
| 23 Trees | 166 |
| 24 Multiplicity | 169 |
| A guide to further reading | 174 |
| Bibliography | 176 |
| Index | 177 |