
THE ART OF COMPUTER SYSTEMS PERFORMANCE ANALYSIS

Techniques for
Experimental Design,
Measurement, Simulation,
and Modeling

RAJ JAIN

Digital Equipment Corporation
Littleton, Massachusetts



JOHN WILEY & SONS, INC.

New York / Chichester / Brisbane / Toronto / Singapore

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