

Edwin Hewitt Kenneth A. Ross

Abstract Harmonic Analysis

Volume I

Structure of Topological Groups

Integration Theory Group Representations

Second Edition



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