

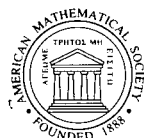
MATHEMATICAL Surveys and Monographs

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The Classification of the Finite Simple Groups, Number 2

Part I, Chapter G: General Group Theory

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Contents

Preface	xi
Part I, Chapter G: General Group Theory	
A. Introduction	1
1. Notation	2
2. Some \mathcal{K} -Group Conditions	4
B. Semisimple Subgroups	6
3. Components and the Generalized Fitting Subgroup	6
4. π -Components and π -Layers	16
5. $L_{p'}$ -Balance and p^* -Groups	23
6. p -Terminality	34
7. Semirigidity	45
8. The Permutation Action of p -Groups on Components	48
C. Nilpotent Groups and Their Extensions	53
9. Modules, Representations, and Cohomology	53
10. Small p -Groups	61
11. Automorphisms of p -Groups and Coprime Action	72
12. p -Constrained Groups	78
13. Solvable Components and Solvable L -Balance	79
14. Goldschmidt-O'Nan Modules	85
D. Fusion and Normal Subgroups	89
15. Abelian Normal Subgroups and Quotients	89
16. Local Control of Fusion	96
E. Uniqueness Subgroups	101
17. Strongly p -Embedded Subgroups and Involutions	101
18. Preuniqueness Subgroups and Standard Components	106
F. The Analysis of Signalizers	110
19. The Bender Method	110
20. The Signalizer Functor Method: k -Balance	118
21. The Signalizer Functor Method: Signalizer Functors	122
22. The Signalizer Functor Method: Connectivity	125
23. Signalizers, p -Constraint and Transitivity Theorems	129
G. Subgroups of Parabolic Type	134
24. The Klinger-Mason Method	135
25. p -Stability and Quadratic Modules	140
26. Thompson Factorization	147
27. Near Components	157
28. The Amalgam Method	161

H. Some Recognition Issues	169
29. Defining Amalgams	170
30. Split BN -Pairs	174
31. Extensions of Extra-special 2-Groups	183
I. Characters and Counting	188
32. Ordinary Character Theory	188
33. Modular Character Theory	195
34. Involutions and Counting Arguments	198
Background References	203
Expository References	204
Glossary	207
Index	210