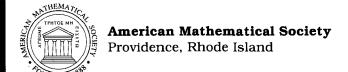
## Translations of

## MATHEMATICAL MONOGRAPHS

Volume 147

## Mixed Problem for Partial Differential Equations with Quasihomogeneous Principal Part

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